



Seminar

Wednesday, 12 June 2024 - h. 14:30

Fisica della Materia room (Department of Physics)

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**“From molecular dynamics to the hydrodynamic limit
using the Distinguishable Kinetic Ising Model”**

Abstract

The lattice Boltzmann method (LBM) is based on the discretization of the Boltzmann transport equation in time, space and momentum. Assuming a convergence to a local Maxwell-Boltzmann distribution, the momentum-space discretization is obtained by means of Gauss-Hermite quadratures which are supposed to capture the equilibrium diffusive/ballistic dynamics of a homogeneous system at thermal equilibrium. However, when trying to derive such discretization from molecular dynamics (MD), i.e. by means of the molecular-dynamics-lattice-gas (MDLG) mapping [1], one can only approximately recover the standard LBM stencils, for certain values of the coarse-graining parameters. Furthermore, while LBM is concerned with the expectation value of the discrete distribution (populations), by means of MDLG one can study their fluctuations displaying non-trivial scaling features [2].

I will introduce a kinetic Ising model with distinguishable particles which offers a possible alternative to the need of extensive and computationally demanding MD simulations required to investigate the different regimes of the MDLG mapping: one can leverage the equivalence between the Ising model and the lattice gas to define a discrete version of MD allowing for phase-separation (still in the correct universality class) and consistent thermodynamic fluctuations.

Distinguishability is necessary to reconstruct the coarse-grained discrete probability distribution (populations) while allowing for local momentum conservation. The model is compliant with the results obtained in [1] and [2] while extending the analysis to different scaling regimes. I will also show that the MDLG populations can capture both a Gaussian and a non-Gaussian statistics according to the value of the coarse-graining parameters, demonstrating non-trivial scale transformation properties that are related to the framework of the Renormalization Group.

[1] : Parsa, M. R. and Wagner, A. J., PRE, 96, 013314 (2017).
[2] : Parsa, M. R. and Wagner, A. J., PRL, 124, 234501 (2020).